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# A Model of Anticipated Consumption Tax Changes

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## What are effects of **preannounced VAT changes** in a model of **durables**?

- ▶ Is  $\tau^c \Downarrow$  asymmetric to  $\tau^c \Uparrow$ ?  
 $\Rightarrow \mathcal{A}. \text{ asymmetric}$
- ▶ Which is better,  $\tau^c \Uparrow$  *once* or  $\tau^c \Uparrow$  with *multiple* times?  
 $\Rightarrow \mathcal{A}. \text{ multiple times}$

**What I do:** construct a life-cycle heterogeneous-agent GE model of **durables** with

$$\mathcal{T}(x^d) = \begin{cases} (1 + \tau^c)x^d & \text{if } x^d \geq 0 \\ x^d & \text{if } x^d < 0, \end{cases}$$

$$\text{where } x^d = d - (1 - \delta^d)d_{-1}$$

To my best knowledge, this is the **first** work that incorporates the **tax wedge** into **macro GE** model to study **anticipated VAT** changes

# Model : Households

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# Households problem

Key Ingredients: **Life-cycle, Hetero, Durables, Tax Wedge**

$$v_j(a_{-1}, d_{-1}, e) = \max_{a, c, d} u(c, d) + \beta \sum_{e'} v_{j+1}(a, d, e') \pi(e'|e)$$

$$\text{s.t. } (1 + \tau^c)c + a + \mathcal{T}(x^d) = (1 + r)a_{-1} + y_j(e) + b$$

$$x^d = d - (1 - \delta^d)d_{-1}$$

$$a \geq 0, \quad (c, d) \geq 0.$$

$\mathcal{T}(\cdot)$ : tax wedge,  $\tau$ : taxes,  $b$ : received bequest,  $y_j(e)$  is given by

$$y_j(e) = \begin{cases} w\kappa_j e & \text{if } j < J^R \\ ss & \text{if } j \geq J^R \end{cases}$$

$ss$ : social security,  $\kappa_j$  age-specific wage component.

# Anticipated VAT Changes:

**Partial Equilibrium:** keeping prices constant

1. Tax Elasticities :  $\epsilon_{C+X_+^D}$  &  $\epsilon_{X_+^D}$ 
  - Baseline Model & Empirics

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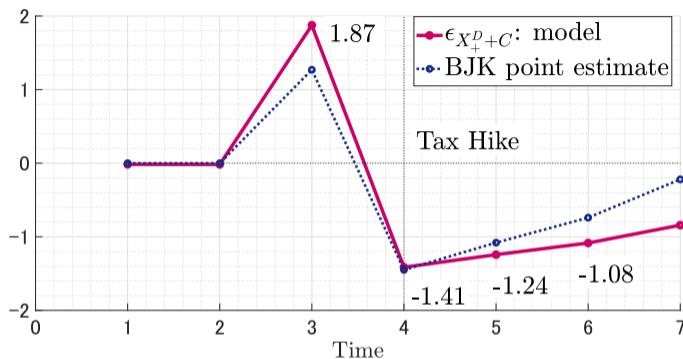
Anticipated VAT Changes:  
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# Tax Elasticities



- ▶ The model  $\epsilon_{C+X^D}$  is within 95% confidence interval reported in [BJK](#)
- ▶  $\epsilon_{X^D}$  one period before  $\tau^c \uparrow$ 
  - ▶ Empirics: 8.1 – 12.8 for **autos** in Baker et al. ('19)
  - ▶ My Model: 10.6
- ▶ Literature found it difficult to match: (Mckay& Wieland '19 etc)

# Counter-Factuals:

1. Counter-Factual 1:  $\tau^c \downarrow$
2. Counter-Factual 2: multi-times  $\tau^c \uparrow$

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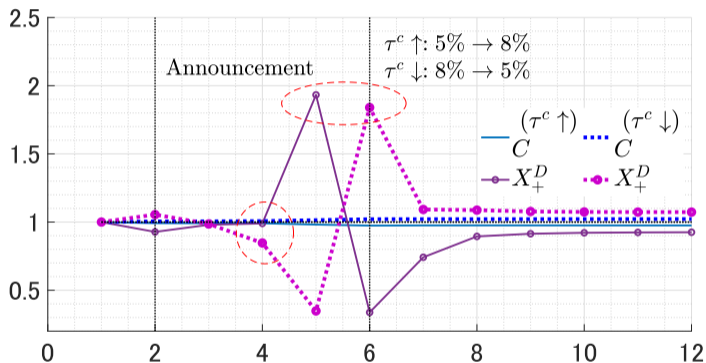
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# Tax Cut: 8% $\rightarrow$ 5%

(Example: Germany & UK, 2020)



## Asymmetric Effects:

- (1) Gradual  $X_+^D \downarrow$  before  $\tau^c \downarrow$
- (2) Magnitude of intertemporal substitution

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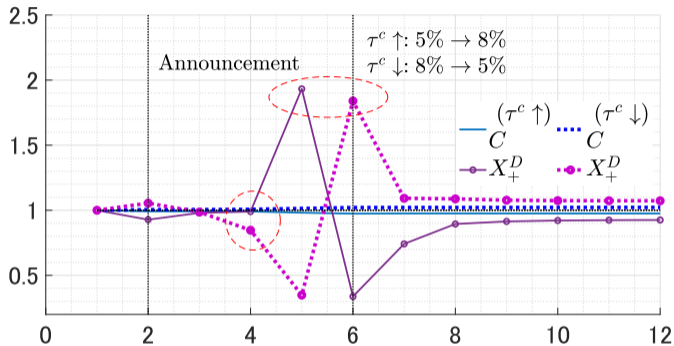
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## Tax Cut: 8% $\rightarrow$ 5%



### Asymmetric Effects: Implications

- ▶ Linearized Solution: won't capture asymmetry
- ▶ Reduced form: should not mix the sample of  $\tau^c \uparrow$  &  $\downarrow$

Germany: temporary cut

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# Multiple-Times Tax Hikes:

*How can we better implement the tax hike?*

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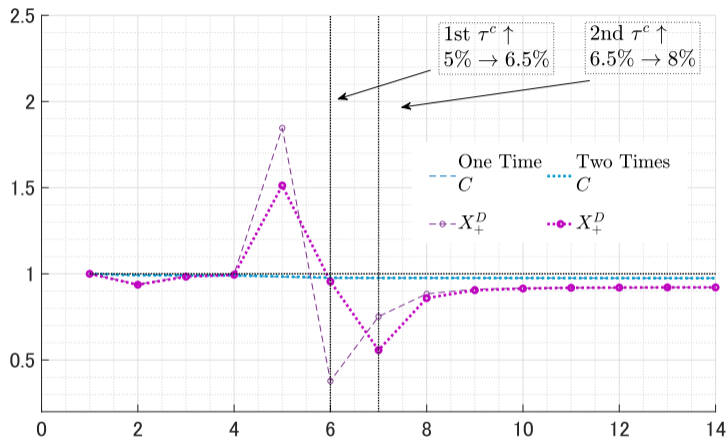
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# One-Time or Two-Times



- Weaker intertemporal shifting
- Put off the plummet

3 times , 2 times welfare .

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[RQ] What are effects of **preannounced VAT changes** in a model of **durables**?

(1) **Tax Wedge** plays a central role:

- ▶ Reproducing **dynamic pattern of empirical tax elasticity**

(2) **Life-cycle**:

- ▶ Low **Elasticity of Durables**
  - ▶  $GE \approx PE$

(3) **Counter-Factuals**:

- ▶  $\tau^c \downarrow$  is **asymmetric** to  $\tau^c \uparrow$
- ▶ Multiple times Tax Hike is welfare improving for most of HHs.

# Appendix: Main Slides for 60+ mins ver.

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(1) **Gov't** budget constraint:

$$G + SS = \tau^c [C + X_+^d]$$

$$\text{where } X_+^d \equiv \sum_j \int_{x_j^d > 0} x_j^d d\mu_j$$

(2) **Firm**: Perfect competition with Cobb-Douglas production

$$r + \delta = F_K(K, N), \quad w = F_N(K, N)$$

(3) Competitive **Dealers** of Durables:

- ▶ manage all durable transactions
- ▶ exist to prohibit direct and private durable trade btw HHs

clearing, flow chart

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# Stationary Equilibrium:

## Parameterization and Baseline Results

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# Parameterization: Japanese Annual Model

parameters	values	meanings	source (annual) <a href="#">▶ why Japan?</a>
$\beta$	0.977	discounting	standard in Japan (e.g. Hayashi and Prescott)
$\sigma$	2.0	inverse IES	standard
$\delta$	0.1	$K$ dep	standard
$\delta^d$	0.15	$D$ dep	expndr share $\times$ each dep rate
$\rho_e$	0.9	persistence in $e$	Nakajima and Takahashi (2017)
$\sigma_e$	0.2072	std in $e$	Lise et al. (2014)
$\{\kappa_j\}$	-	age-depend't earnings	Yamada (2011)
$\tau^{ss}$	0.64	social security	report from OECD
$q$	1.0	resale value	-

$$u(c, d) = \frac{\left(c^\theta (d + \epsilon^d)^{1-\theta}\right)^{1-\sigma}}{1-\sigma}$$

Non-Homothetic Utility

to reproduce hump shape in  $x^d$  profile.

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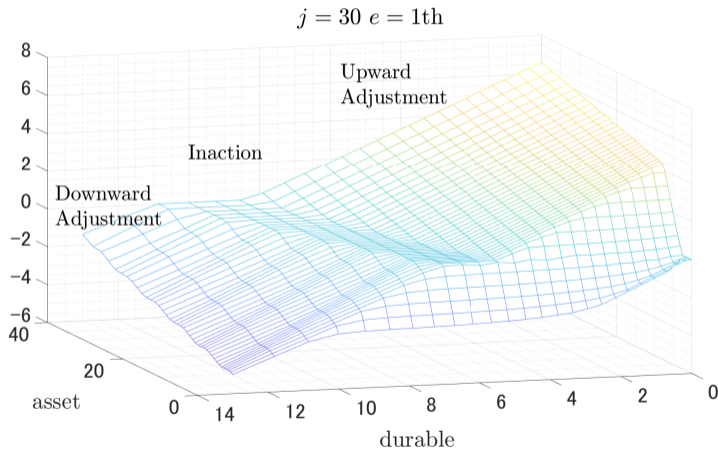
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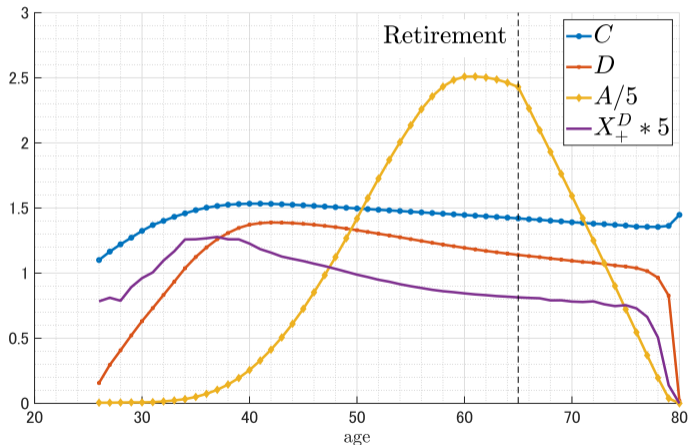
# (S,s) Rule due to Tax Wedge

$$x_j^d = g_j^d(a_{-1}, d_{-1}, e) - (1 - \delta^d)d_{-1}$$

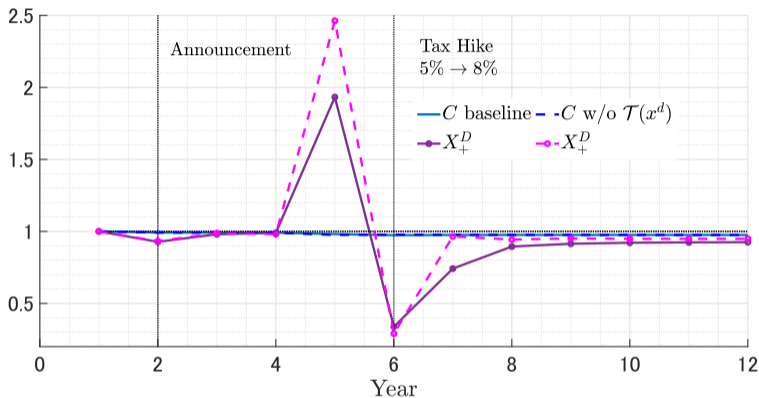


# Life-cycle Profiles

Average Life-cycle (10,000 HHs per cohort  $\times$  55 cohorts)



# Roles of Tax Wedge: Comparison in IRF



- $X_+^D(t)/X_+^D(1)$  and  $C(t)/C(1)$  are shown
- A model without the tax wedge  $\mathcal{T}(x^d)$ :  $q = (1 + \tau^c)$

sensitivity:  $\delta^d$

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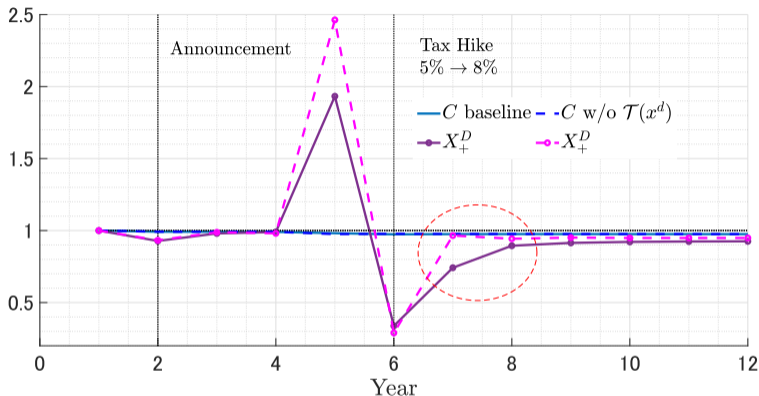
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# Roles of Tax Wedge: Comparison in IRF



► After  $\tau^c \uparrow$ : *slow* convergence

consistent to BJK.

Sensitivity: other Inv't frictions, unanticipated  $\tau^c \uparrow$ .

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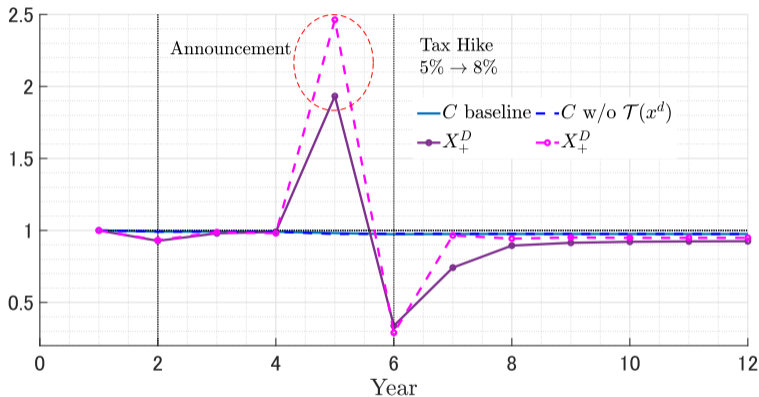
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# Roles of Tax Wedge: Comparison in IRF



The model w/o tax wedge predicts  $X_+^D$  overly

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# Why a Model w/o Tax Wedge Predicts $X_+^D$ Overly?

- ▶ Budget in a model w/o tax wedge (i.e. assuming  $q = 1 + \tau^c$ )

$$(1 + \tau^c)(c + x^d) + a = (1 + r)a_{-1} + y_j + b$$

- ▶ Why?  $\Rightarrow$  **A chance of (unrealistic) revenue over the dynamics**

- ▶ Example:

- ▶ **Buy** the durables before the tax hike ( $t = 5$ )  $1 + \tau^c = 1.05$ ,

$$1.05[c + \underbrace{x^d}_{>0}] + a = (1 + r)a_{-1} + y_j + b$$

- ▶ **Sell** them in tax hike ( $t = 6$ )  $1 + \tau^c = 1.08$ ,

$$1.08c + a = (1 + r)a_{-1} + y_j + b \underbrace{-1.08x^d}_{>0 \because x^d < 0}$$

- ▶ **Revenue** of stockpiling:  $8 - 5 = 3\%$
- ▶ Costs of stockpiling:  $\delta^d$  and utility fluctuation

$\Rightarrow$  As tax hike is larger scale or  $\delta^d$  is sufficiently lower, this **misspecification** problem becomes more critical.

large tax hike

bias in estimation

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# General Equilibrium :

*How is it different from Partial Equilibrium ?*

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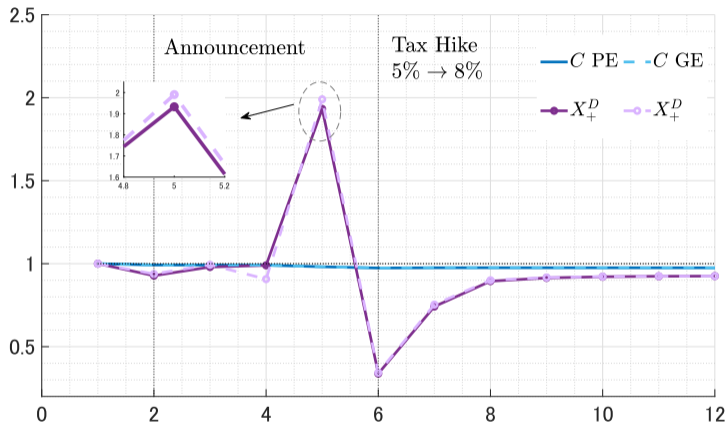
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► very **similar** :  $GE \approx PE$

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# Why so similar?

Koby and Wolf (2020): “**interest rate elasticity** is **sufficient statistics** for whether  $GE \approx PE$ ”

$$u'(c) \geq \beta \frac{1 + \tau^c}{1 + (\tau^c)'} (1 + r') u'(c)$$

Tax elasticity  $\approx$  **Interest rate elasticity** (c.f. Correia et al. 2008)

- ▶ **Puzzle:** Standard (S,s) models generate too high elasticity
  - ▶ Literature: Koby & Wolf ('20), McKay & Wieland ('19), Winberry ('20)
- ▶ My Model: *Low* **interest rate elasticity**
  - (1) **Life-cycle:** mass of HHs who're less responsive
    - ▶ The young buy the durables, regardless of  $r$ .
    - ▶ The old do not buy the durables, regardless of  $r$ .
  - (2) **Two assets:** (c.f. Berger and Vavra 2015, Bachmann and Ma 2013)
    - ▶ Khan and Thomas (2008): HHs smooths  $C \Rightarrow$  smooth  $I$ .
  - (3) **High depreciation rate**  $\delta^d$  (c.f. House 2014)

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Table: Interest Rate Elasticity of Durable: (from Mckay & Wieland '19)

<b>Data</b>	
Baker et al. ('19)	1.1
Mian and Sufi ('12)	4.3 – 5.0
<b>Models</b>	
Infinitely Lived + Fixed cost (Mckay & Wieland '19)	47.7
My baseline	4.1

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## No.6105 課税の対象

[令和2年4月1日現在法令等]

消費税の課税対象は、国内において事業者が事業として対価を得て行う資産の譲渡等及び外国貨物の引取り（輸入取引）です(注)。

### 1 国内において事業者が事業として対価を得て行う資産の譲渡等

#### (1) 事業者が事業として行う取引

「事業者」とは、個人事業者(事業を行う個人)と法人をいいます。

「事業として」とは、対価を得て行われる資産の譲渡等を繰り返し、継続、かつ、独立して行うことをいいます。

したがって、個人の中古車販売業者が行う中古車の売買は事業として行う売買になりますが、給与所得者がたまたま自分の自家用車を手放す行為などは、事業として行う売買とはなりません。

なお、法人は事業を行う目的をもって設立されたものですから、その活動はすべて事業となります。

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## Consumption Tax

### No.1 Taxable Sales

Consumption tax is levied on "Taxable Sales". "Taxable sales" mean sales that satisfy all of the following four conditions.

- (1) Effectuated in Japan
- (2) Effectuated by a business for its business purposes
- (3) Effectuated for a compensation
- (4) Effectuated by the transfer or lease of assets or by the provision of services

(Referred to as "transfer of assets etc.")

For example, machinery rental fees and proceeds from the sale of machinery, buildings and other business assets are included in taxable sales in addition to such things as proceeds from sales of products, contract work and services.

## How VAT works



**You can only charge VAT if your business is registered for VAT.**

VAT is charged on things like:

- business sales - for example when you sell goods and services
- hiring or loaning goods to someone
- selling business assets
- commission
- items sold to staff - for example canteen meals
- business goods used for personal reasons
- 'non-sales' like bartering, part-exchange and gifts

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## Why Japan?

- ▶ Japan's case in 2014 (5% → 8%) was relatively good environment:
  - ▶ A **single flat** rate
    - ▶ No **reduced** tax, unlike EU countries
  - ▶ **Full pass-through**: Gov't forced it in 1997 and 2014 but not in 2019. *See next page*
- ▶ The huge government debt necessitates large scale fiscal reform in Japan.

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# Detail on Full Pass-Through

- ▶ Gov't was mainly concerned about **unfair pass-through** *between firms* with unequal negotiation power.
- ▶ Ministry of Finance, FTC, Consumers Affairs Agency published an official guideline in cooperation to **prohibit non-full pass-through**.
  - ▶ Firms are **not** allowed to discount their product **because of the tax hike**.
    - ▶ ✕ “Discount by the tax increase”
    - ▶ ✕ “A special sale for tax hike”
    - ▶ ○ “Seasonal sale”
    - ▶ ○ “Clearance sale”
- ▶ Price-setting behavior is affected in other countries (e.g. Karadi and Reiff 2018)

[https://www.mof.go.jp/tax\\_policy/summary/consumption/250910tenka.htm](https://www.mof.go.jp/tax_policy/summary/consumption/250910tenka.htm) in Japanese (plz use translation in the browser)

## ► **Consumption Tax** including **Unconventional Fiscal Policy**

### ► **Theory**

Nishiyama and Smetters (2005), Correia (2010), Correia et al. (2013), Baker et al. (forthcoming), Parodi (2019a, 2019b), etc

### ► **Empirics**

Cashin and Unayama (2016a,b), Cashin (2017), D'Acunto, Hoang and Weber(2016,2018), Baker et al. (2019), etc

⇒ **Incorporate durables & tax wedge into GE to study anticipated VAT changes**

## ► **Lumpy Durables** or **Life-cycle Durables**

### ► **Lumpy Durables**

Lam (1989, 1991), Berger and Vavra (2014,2015), Guerrieri and Lorenzoni (2017), McKay and Wieland (2020), Zorzi (2020), etc

### ► **Life-cycle Durables**

Attanasio (1999), Fernández-Villaverde and Krueger (2007, 2011), etc

⇒ **Life-cycle and tax wedge are key components to match the elasticity** [back](#)

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# Choice-Specific Value Functions

$$\begin{aligned}v_j^{up}(a_{-1}, d_{-1}, e) &= \max_{c, a \geq 0, x^d \geq 0} u(c, d) + \beta \mathbb{E}[v_{j+1}(a, d, e')|e] \\ \text{s.t. } (1 + \tau^c)[c + x^d] + a \\ &= (1 + r)a_{-1} + y_j(e) + b \\ x^d &= d - (1 - \delta^d)d_{-1}\end{aligned}$$

$$\begin{aligned}v_j^{down}(a_{-1}, d_{-1}, e) &= \max_{c, a \geq 0, x^d < 0} u(c, d) + \beta \mathbb{E}[v_{j+1}(a, d, e')|e] \\ \text{s.t. } (1 + \tau^c)c + qx^d + a \\ &= (1 + r)a_{-1} + y_j(e) + b \\ x^d &= d - (1 - \delta^d)d_{-1}\end{aligned}$$

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# Equilibrium: Market Clearing and Dealers

Factors and goods markets clear

$$\begin{aligned} \text{(i)} \quad K &= \sum_{j=0}^J \int a d\mu_j, & \text{(ii)} \quad N &= \sum_{j=0}^{J^R-1} \int \kappa_j e d\mu_j \\ \text{(iii)} \quad C + X^D + G + K' &= K^\alpha N^{1-\alpha} + (1 - \delta)K. \end{aligned}$$

where  $X^D \equiv X_+^D + qX_-^D$ .

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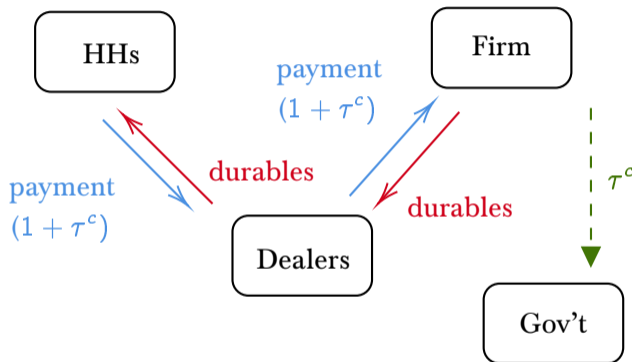
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# Flow Chart: Buying New Durables



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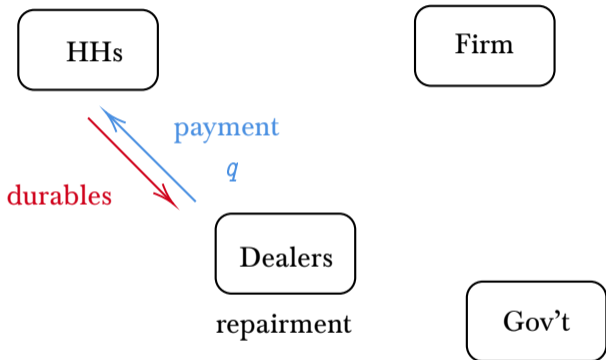
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# Flow Chart: Selling Durables



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# Non-Homothetic Utility

**Problem:** Standard homothetic utility functions do not generate hump shape in  $x^d$  profile.

⇒ **Stone Geary:**

$$u(c, d) = \frac{\left(c^\theta (d + \epsilon^d)^{1-\theta}\right)^{1-\sigma}}{1 - \sigma}$$

With  $\epsilon^d > 0$ ,  $d$  is **luxury** ⇒ *The rich buy more durables*

- ▶ Helps generate **hump-shaped**  $x^d$  profile
  - ▶ because the middle-age are rich in both asset and earnings

**Calibration:**  $\theta$  and  $\epsilon^d$  are calibrated matching (i)  $X^D/C$  share and (ii) peak and initial  $x^d$  profile ratio. [back](#)

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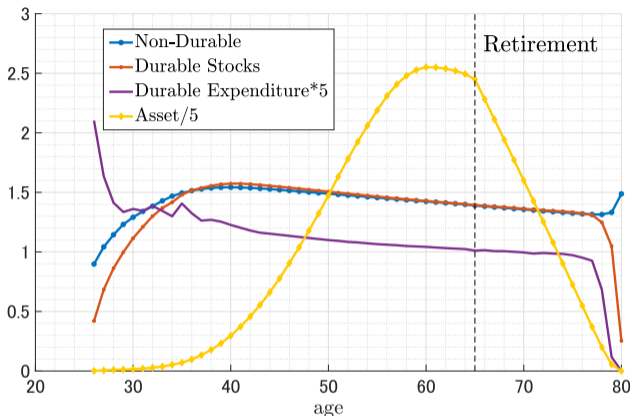
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# Life-cycle Profiles: Cobb-Douglas Case



- Roughly, durable expenditure is **decreasing in age**
- **Share btw  $c$  &  $d$  are constant** once borrowing const becomes slack.
- some durable stocks at the end of life

# Wealth Distributions: Untargeted

Table: Wealth Share owned by each quintile

	1st	2nd	3rd	4th	5th	top10%	top1%
Data	0.3%	3.7%	9.8%	21.3%	64.9%	45%	10.2%
Baseline	0.1%	2.4%	12.6%	27.3%	57.6%	35.8%	5.7%

Data:

National Survey of Family Income and Expenditure in 2014 by Kitao and Yamada (2019)

Why is asset distribution important here?

- ▶ HHs cannot afford stockpiling of durables w/o assets.
- ▶ Heterogeneous welfare costs depend on assets.

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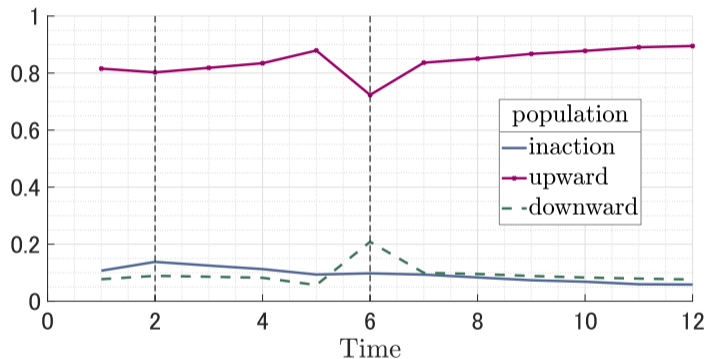
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# Baseline Results: Extensive Margin



- Extensive margin does not change much

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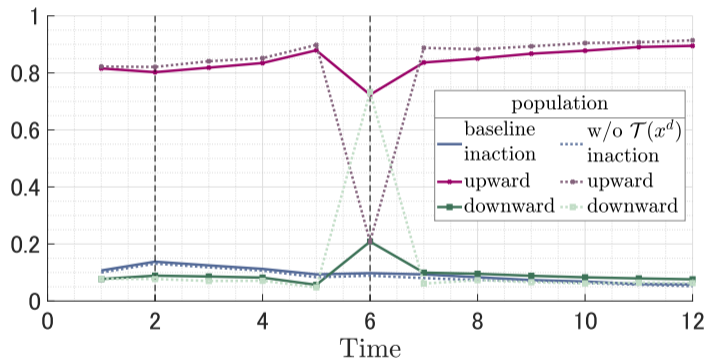
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# Baseline Results: Extensive Margin



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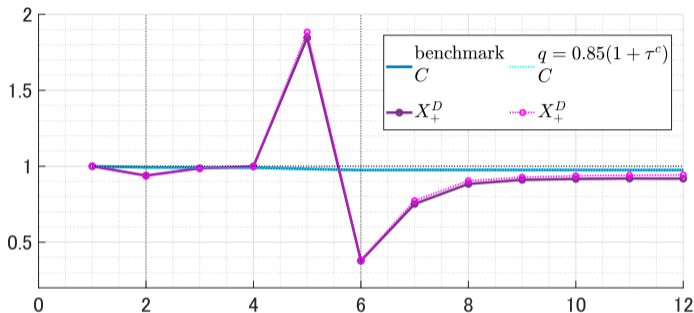
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# Tax Wedge & Partial Irreversibility



$$\mathcal{T}(x^d) = \begin{cases} (1 + \tau^c)x^d & \text{if } x^d \geq 0 \\ 0.85(1 + \tau^c)x^d & \text{if } x^d < 0, \end{cases}$$

Benchmark (Tax Wedge)  $\approx$  Traditional partial irreversibility.

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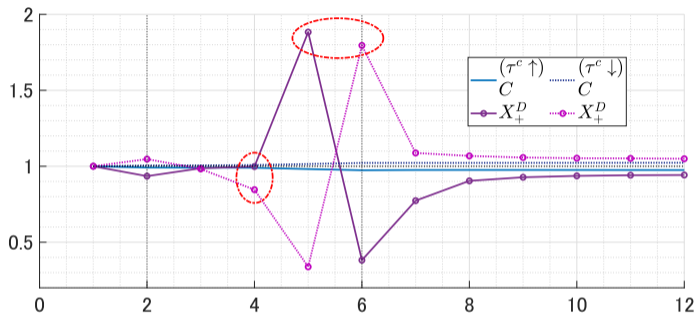
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# Partial Irreversibility: Asymmetricity Result



$$\mathcal{T}(x^d) = \begin{cases} (1 + \tau^c)x^d & \text{if } x^d \geq 0 \\ 0.85(1 + \tau^c)x^d & \text{if } x^d < 0, \end{cases}$$

Asymmetric Result arises in the (traditional) partial irreversibility.

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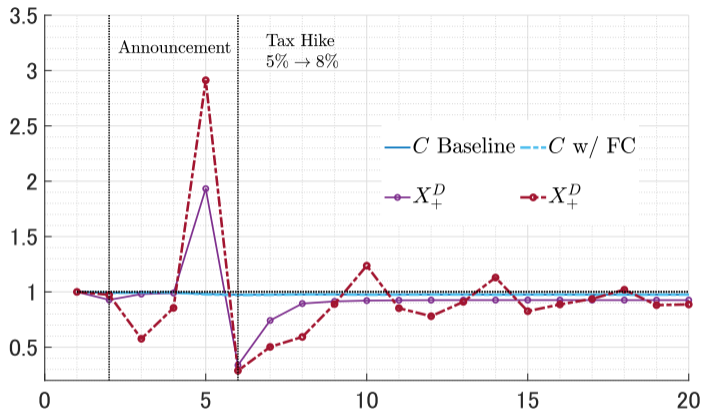
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# Other Costs: Fixed Cost



Fixed costs:  $F(d, d_{-1}) = \mathbb{I}_{x^d \neq 0} F^d (1 - \delta^d) d_{-1}$

- bigger spike
- negative persistence  $\Rightarrow$  overshooting in period 10, 14, 18.

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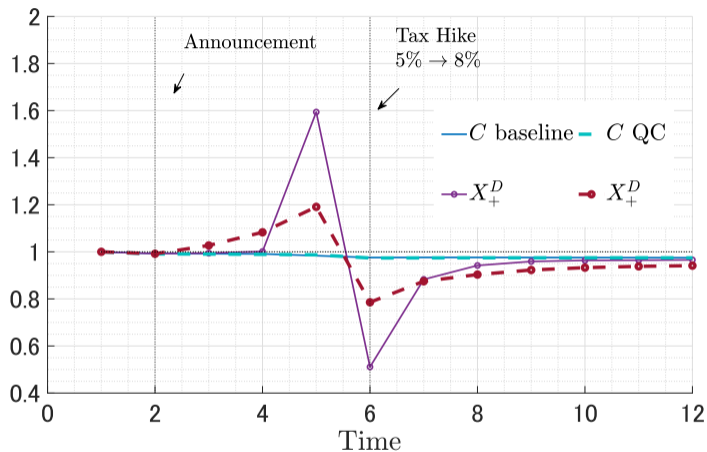
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# Other Costs: Quadratic Adjustment Cost



Quadratic Adjustment Costs:  $QC(d, d_{-1}) = \frac{F^{qc}}{2} [d - (1 - \delta^d)d_{-1}]^2$  [Back:IRF](#)

- ▶ smaller spike
- ▶ slow adjustment before  $\tau^c \uparrow$

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# IES estimation: Cashin and Unayama (2016)

**Empirics:** Cashin and Unayama (2016 REStat) and Cashin (2018)

- ▶ Both estimated IES with Rep. HH model of durables and VAT w/o tax wedge.
- ▶ **Their result:**  $IES (= 1/\sigma) = 0.21$

**My Result:** overshoot in a model w/o tax wedge .

- ▶ To compromise with observed *small* stockpiling behavior, they must have low IES.
- ▶  $\Rightarrow$  *their estimation result underestimates the IES.*

Back:overly prediction

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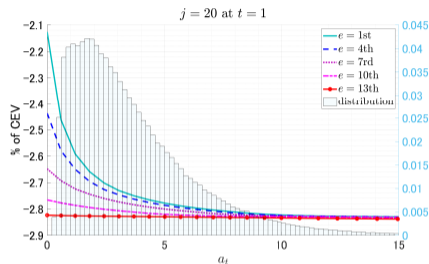
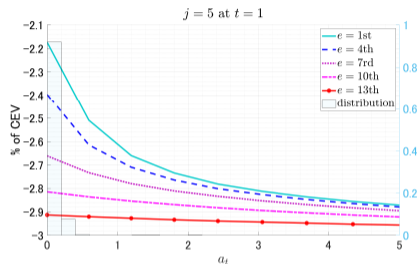
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# Welfare (CEV) over dynamics



**Tax-induced inflation**  $\Rightarrow$   $\downarrow$  real value of (i) Asset (ii) Durable (iii) Labor Earning

$\Rightarrow$  **Progressive**

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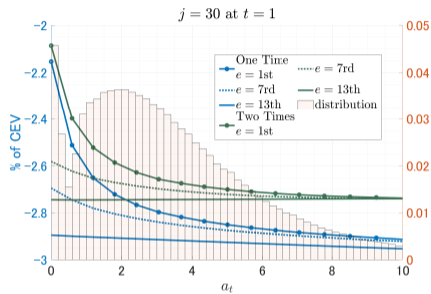
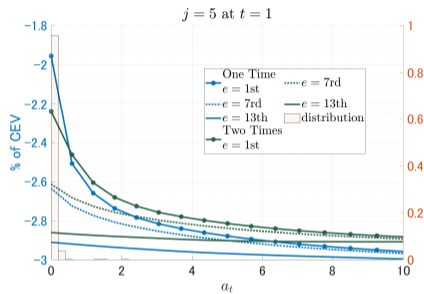
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# Welfare Comparison: once or 2 times



- Two-times-hikes scheme **mostly welfare dominates** one-time-hike scheme
  - **exception:** young poor both in asset and earnings

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# Solution Method:

## Nested EGM

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# Byproduct: Numerical Solution

## Two Main Difficulties:

1. **Multi-dimensions**: asset, non-durable and durable.
2. **Discrete choices**: non-concave value function
  - ▶ non-differentiable regions  $\Rightarrow$  derivative based method  $\times$
  - ▶ extremely smoothing interpolation  $\times$
  - ▶ possibly many local maxima (c.f. Iskhakov et al. (2017))

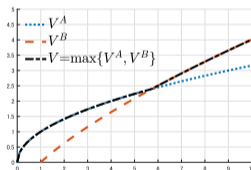


Figure: An image of 1D value function w/ discrete choice

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## Two Main difficulties :

1. **Multi-dimension:** durable, non-durable and asset
2. **Discrete choice:** non-concave value function
  - ▶ non-differentiable regions  $\Rightarrow$  derivative based method  $\times$
  - ▶ extremely smoothing interpolation  $\times$  (c.f. Chebyshev)
  - ▶ possibly many local maxima (c.f. Iskhakov et al. (2017))

**Nested EGM** (Druehl 2019) solves this class of models fast.

1. **Nesting the timing:** Converting the multidimensional problem to *unidimensional*.
2. **Upper Envelope Algorithm:** to identify the *global* maximum

# Advantage of NEGM: How fast?

Table 1: Speed and Accuracy

	VFI	NVFI	NEGM	NVFI+	NEGM+
<i>relative Euler errors</i>					
All (average)	-4.245	-4.173	-4.268	-4.173	-4.268
5th percentile	-5.811	-5.691	-5.908	-5.691	-5.908
95th percentile	-2.689	-2.708	-2.715	-2.708	-2.715
Adjusters (average)	-4.232	-4.352	-4.502	-4.352	-4.502
Keepers (average)	-4.247	-4.140	-4.225	-4.140	-4.225
<i>timings (in minutes, best of 5)</i>					
<u>Total</u>	<u>63.54</u>	5.96	<u>4.12</u>	4.71	1.45
Post-decision functions	0.00	1.75	3.53	0.49	0.82
Keeper problem	62.26	4.19	0.57	4.20	0.61
Adjuster problem	1.28	0.02	0.02	0.02	0.02
Speed-up relative to VFI		10.66	15.42	13.49	43.85

Druehl (2019) uses Berger and Vavra (2015) as a benchmark model:

- ▶ NEGM is **15 times faster** than traditional VFI.
- ▶ Speed gain is mostly from **nesting** (but not EGM).
- ▶ As accurate as VFI

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# Nesting: Overview of Algorithm

- ▶ Beginning: HH know states.
- ▶ **1st decision:** Solve **inaction problem** first, and get  $c^{inact}(m, d, e)$  using **EGM** with **Upper Envelope Algorithm** to find *global optim.*
- ▶ **2nd decision:** HH solves optimal adjusting ( $i \in \{\text{up, down}\}$ ) problem

$$\begin{aligned} v_j^i(\cdot) &= \max_{\textcolor{red}{d}} u(c, d) + \beta \mathbb{E} v_{j+1}(\cdot) \\ \text{s.t. } &(1 + \tau^c)c + Q^i d + a = m^i \\ &c = c^{inact}(m^i - Q^i d, d, e) \\ &x^d \leq 0, \quad a \geq 0 \end{aligned}$$

where  $m^i$  is choice-specific COH,  $Q^i \in \{(1 + \tau^c), q\}$ .

Both 1st and 2nd problem is **unidimensional**.  $\Rightarrow$  unidimensional techniques (interpolation, optimization, etc.).  $\Rightarrow$  curse of dim  $\downarrow$ .

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# Further Extra Appendix:

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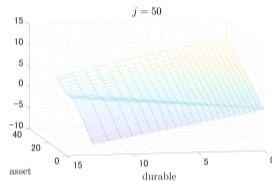
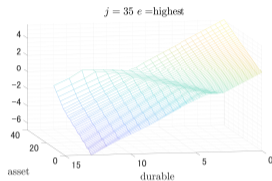
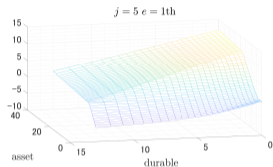
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# Age-dependence in Policy Functions



## Some Caveats

- In life-cycle model, **almost everywhere** can be thresholds of  $(S, s)$  over  $(a_{-1}, d_{-1})$ .

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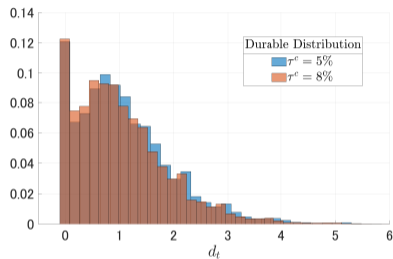
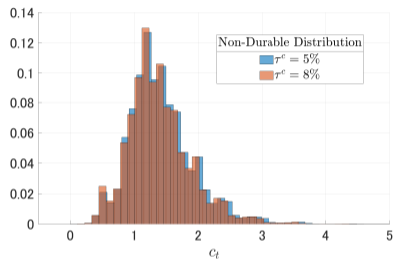
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# Cross-Sectional Effect: Stationary Eq



- **Non-Durable:** Left skewed for all
- **Durable:** Left skewed and higher concentration around center.

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# Elasticity: Yearly $\Leftrightarrow$ Monthly

**Issue:** Model is annual but Baker et al. (forthcoming) is monthly.

1. Solve the perfect foresight with  $\tau^c \uparrow$  by 12%
2. Get a sequence of  $\{X_+^D(t)\}_{t=1}^T$  where  $X_+^D(1)$  is stationary eq value.
3. Compute elasticity  $\epsilon^D|_{12\%}$ :

$$\epsilon^D|_{12\%} = \log X_+^D(t) - \log X_+^D(1)$$

4. This is elasticity when tax change is by 12%. Thus, divide by 12:

$$\epsilon^D|_{1\%} = \frac{\epsilon^D|_{12\%}}{12}$$

5. I report this  $\epsilon^D|_{1\%}$

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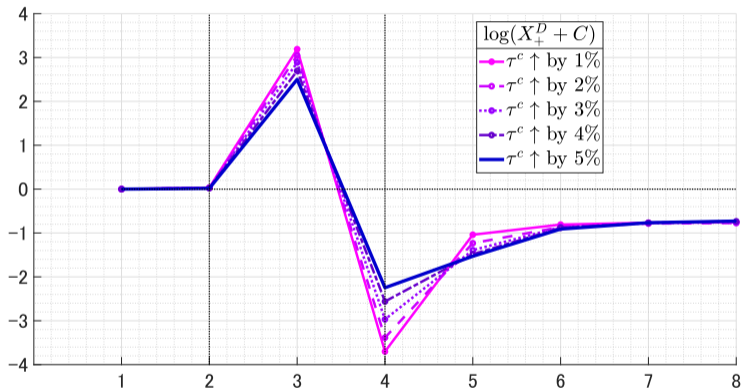
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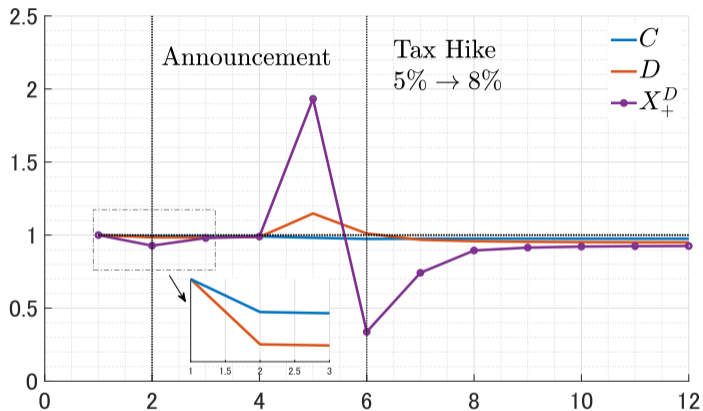
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# Tax Elasticity with Different $\tau^c \uparrow$

The model-implied Tax Elasticity with different  $\tau^c \uparrow$



## Baseline Results: 5% $\rightarrow$ 8%



- $X_+^D(t)/X_+^D(1)$  and  $C(t)/C(1)$  are shown

**Negative income effect** in announcement.

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## Consumption Equivalent Variation: $\omega$

- ▶ Economy A: tax hike
- ▶ Economy B: no policy change (i.e. stay stationary eq)

$$\int \mathbb{E}_t \tilde{v}(\{(1 + \omega)c^A, d^A\}_{j \geq t}^J) d\mu = \int \mathbb{E}_t \tilde{v}(\{c^B, d^B\}_{j \geq t}^J) d\mu$$

$$\text{where } \tilde{v}(\{c, d\}_{j \geq t}^J) = \sum_{j \geq t}^J \beta^j u(c, d)$$

- ▶ The premium  $\omega$  can be thought of as *the percent of life-time non-durables* HHs in economy A lose in welfare term due to the tax hike.
- ▶ Computing  $\omega$

$$\omega(j, a_{-1}, d_{-1}, e) = \left( \frac{v_j^B(a_{-1}, d_{-1}, e)}{v_j^A(a_{-1}, d_{-1}, e)} \right)^{\frac{1-\sigma}{\theta}}$$

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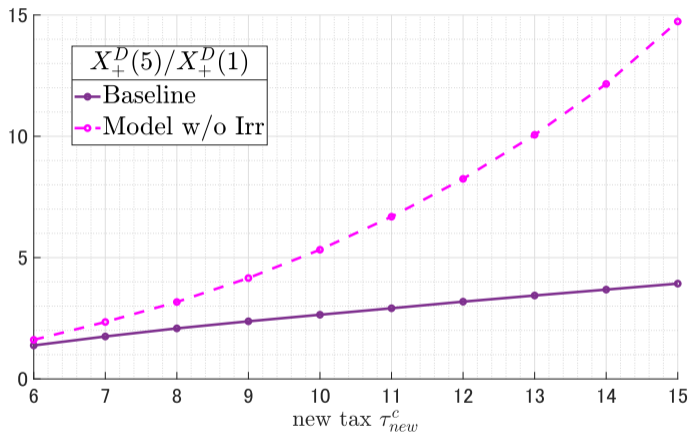
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# How Stockpiling differ with different new tax?



Misspecification becomes critical as tax differential  $\tau_{new}^c - \tau_{old}^c$  increases

(Note 10 in y-axis means 10 times more  $X_+^D(5)$  than  $X_+^D(1)$ , but not 10%  $\uparrow$ )

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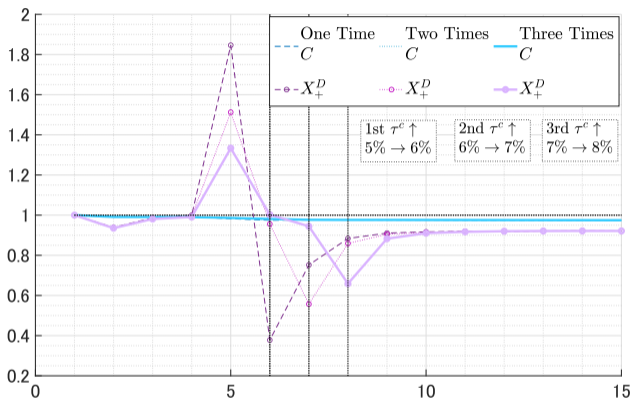
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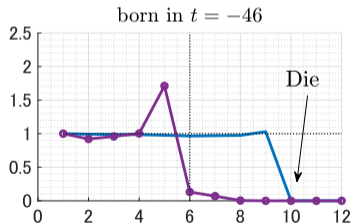
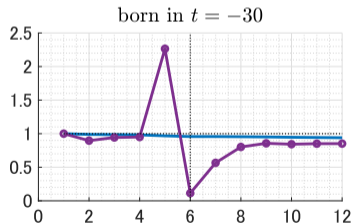
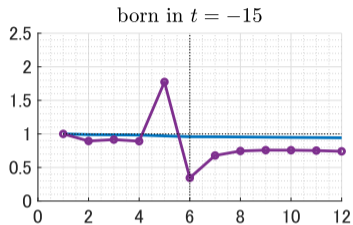
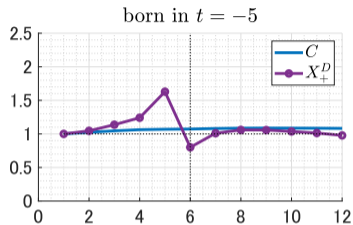
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# Consecutive Multiple Tax Hikes: Three Times



- Weaker intertemporal shifting.
- Put off the plummet

# Age-Dependent Stockpilings



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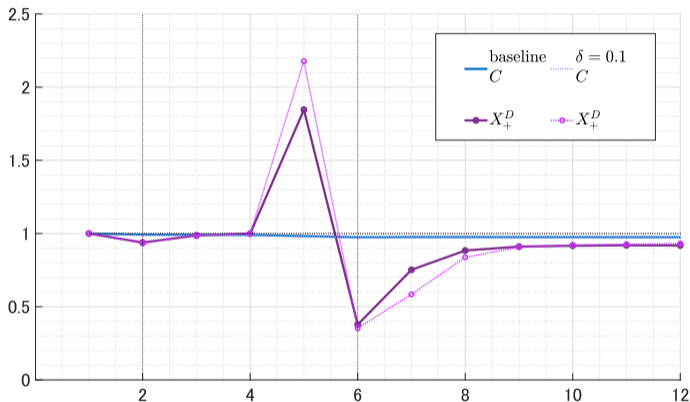
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# Choice of $\delta^d$ :

baseline  $\delta^d = 0.15$



Both are baseline models (w/ tax wedge). [back](#)

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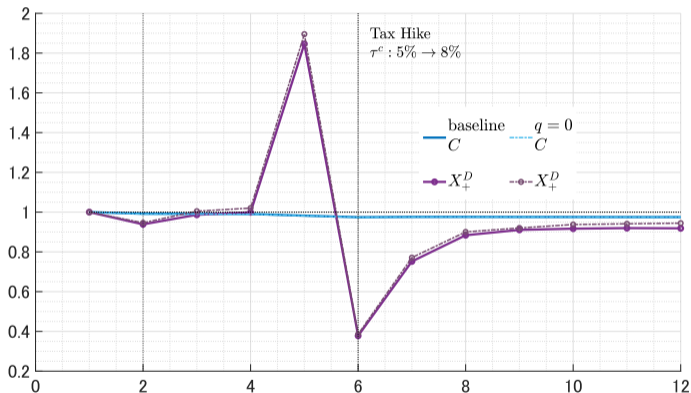
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# Choice of $q$

baseline  $q = 1$



Choice of value of  $q$  does not change the quantitative result almost at all [back](#)

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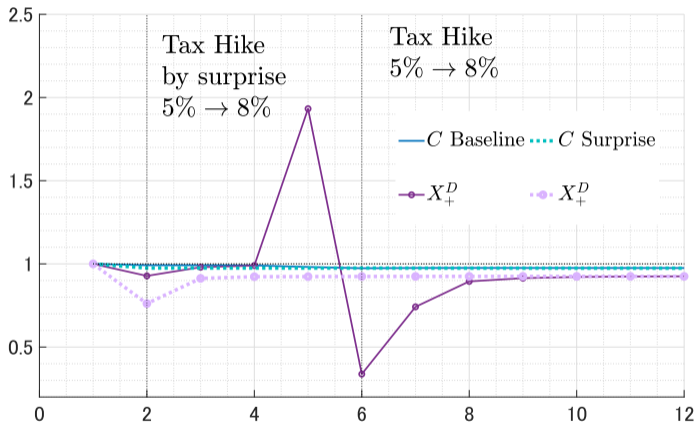
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# No Announcement: Tax Hike



Negative Income Effect only when  $\tau^c \uparrow$  is surprise

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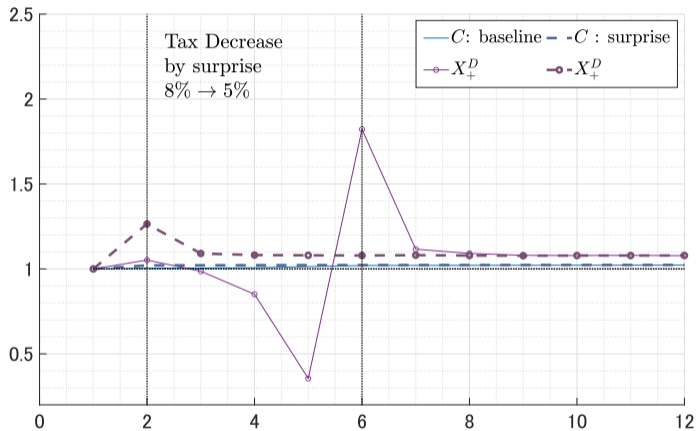
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# No Announcement: Tax Decrease



Almost symmetric to tax hike by surprise. (see previous page)

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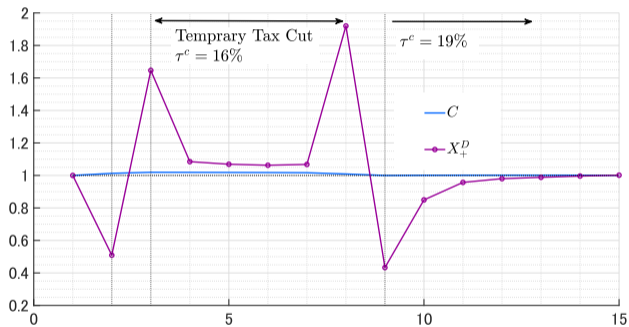
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# Temporary Tax Cut: Germany

19%  $\rightarrow$  16% for a half year



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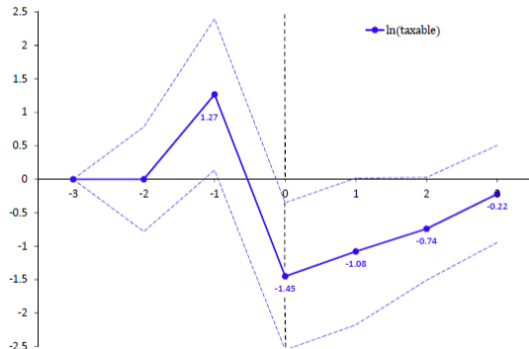
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# Empirical Tax Elasticity: BJK

## Key patterns

- ▶ before  $\tau^c \uparrow$ : sharp response
- ▶ after  $\tau^c \uparrow$ : *gradual* response



from **Baker Johnson Kueng** (forthcoming in AEJ Ma)

(also observed in Baker et al 2019; Mian & Sufi 2012)

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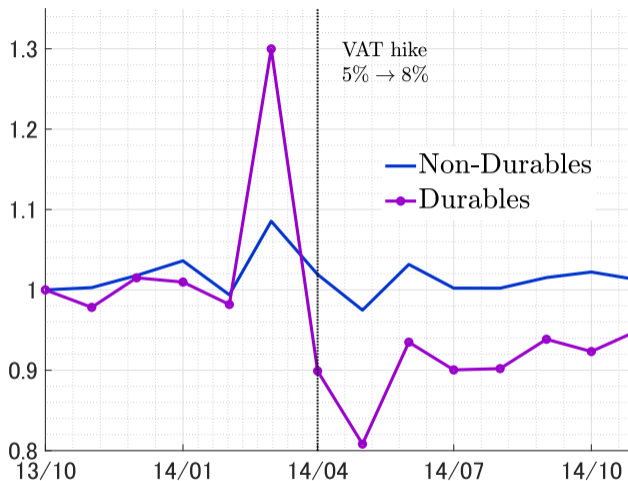
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# Japan: VAT 5% $\rightarrow$ 8%



Seasonally Adjusted. Non-Durable and Durable Spendings

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# Relative Price btw ND and D

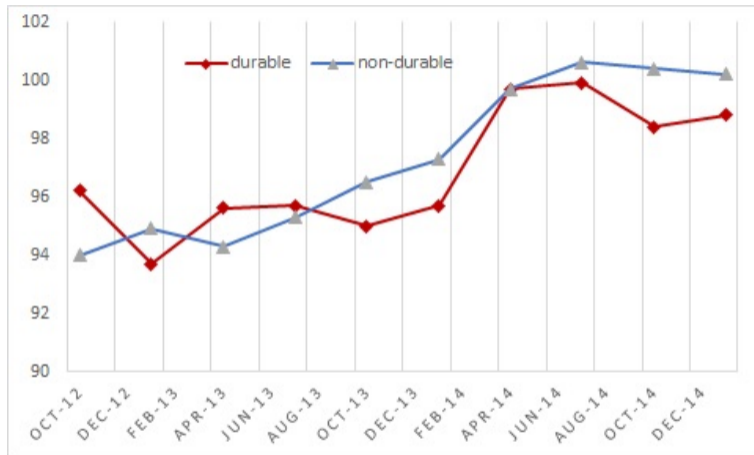


Figure: Consumer Price Indices for both Durable and Non-Durable Goods. Announcement is in October 2012 and Implementation is in April 2014.

Introduction

Model

Main Results

Concluding  
Remarks

Backup Slides

(0) Main Slides for 60 mins  
ver

(1) Primary Appendix

(2) Computation: EGM

(3) More Extra Results

(4) Some Complementary  
Data